# A Monopolistic Competition Model of the Horticultural Industry with a Risk of Harmful Plant Invasion 

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## Introduction

- Growth in demand has led to expansion of the horticulture industry but has increased the risk of invasion by exotic plants (Reichard \& White 2001)
- We model the North American horticulture industry using a monopolistic competition approach
- Also estimate the probability that a new introduced exotic species will become invasive, based on duration data and the characteristics for a sample of exotic plants
- We derive the privately \& socially optimal number of nurseries and determine the appropriate tax rate (annual license fee) for the industry, or introducer pays tax
- We extend the work of Knowler \& Barbier (2005) and revise and update a preliminary version of this research


## Horticulture industry model

- Dixit-Stiglitz monopolistic competition fits the "stylized facts" of the horticulture industry (Dixit \& Stigitz 1977)
- Consumers prefer a variety of differentiated plants, including exotic, imported species
- Firms ("nurseries") are vertically integrated
- An integrated nursery firm imports plant material, propagates it and sells this differentiated product in the retail market
- Estimate the representative firm's profit function, based on data from the US and Canadian horticulture industries


## Modeling assumptions

- Nursery firms import new exotic plant species as a onetime fixed cost, $\boldsymbol{F}$, and produce a unique bundle of plants under increasing returns to scale
- Consumers maximize utility from the "nursery good" and a homogenous composite good
- Consumer preference for a variety of nursery goods is captured by the parameter $\gamma$, which measures substitutability between different plant bundles, with $0<\gamma<1$ and $\sigma=1 /(1-\gamma)>1$ is elasticity of substitution
- We also assume that the industry is constrained by regional resource availability, $L$, measured in labor units


## Private industry equilibrium

- In the short run, each firm's profits are inversely related to the total number of nurseries, $\boldsymbol{n}$, in the industry:

$$
\pi(n)^{s}=\frac{1-\gamma}{\gamma}\left(\frac{L}{n}-F\right), \quad 0 \leq \gamma \leq 1
$$

- In the long run, industry profits are zero, and the privately optimal number of nurseries is:

$$
n^{p}=\frac{(1-\gamma) L}{F}
$$

## Social welfare (I)

- Considering industry output only, then social welfare is the sum of consumers' and producers' surplus:

$$
W(n)=S(n)+\Pi(n)
$$

- Consumer surplus is:

$$
S(n)=\left(\frac{1-\gamma}{\gamma}\right)\left(\frac{a}{\gamma}\right)^{\frac{\gamma}{\gamma-1}} n=D n, \quad D=\left(\frac{1-\gamma}{\gamma}\right)\left(\frac{a}{\gamma}\right)^{\frac{\gamma}{\gamma-1}}
$$

where ' $a$ ' is marginal labor cost of production

- Social welfare in this case is: $W^{\prime}\left(n^{s}\right)=0$


## Social welfare (II)

- For a social optimum, we must also consider the expected social costs from the risk of a harmful plant invasion
- The risk of a newly imported exotic species becoming invasive can be analyzed as a duration problem
- Such problems are characterized by a hazard rate:

$$
h(t)=\lim _{\Delta t \rightarrow 0}\{\mathrm{P}(\text { plant invades in }(t, t+\Delta t] \text { plant has not invaded by } t) / \Delta t\}
$$

- The hazard rate for species $k$ depends on the number of nurseries selling the plant, $n(t)$, and plant attributes, $a_{k}$ :

$$
h(t)=\varphi\left(n(t), a_{k}\right), \varphi_{n}>0
$$

## Stochastic optimization problem

- Invasion damages, $G(\tau)$, are a function of the random time of invasion, $\tau$ :

$$
G(\tau)=\int_{\tau}^{\infty} e^{-\delta(t-\tau)} c A(t) d t
$$

where $A(t)$ is area invaded and ' $c$ ' is average damage per ha invaded

- The social planner maximizes the expected present value of welfare:

$$
\left.\max _{n} J=E\left\{\int_{0}^{\tau} W(n(t)) e^{-\delta t} d t-G(\tau)\right) e^{-\delta \tau}\right\}
$$

where the expectation is taken with respect to $\tau$

## Deterministic optimization problem

- Reed and Heras (1992) transform this problem into deterministic optimal control by introducing a new state variable, $y(t)$, with:

$$
\frac{d y}{d t}=h(t)=\varphi\left(n(t), a_{k}\right): \quad y(0)=0
$$

- The stochastic problem now forms a standard deterministic optimal control problem:

$$
\left.\max _{n} J=\int_{0}^{\infty} e^{-\delta t-y(t)}[W(n(t))+\delta G(\tau))\right] d t
$$

subject to the above equation of motion

## Welfare maximizing equilibrium and tax

- Condition for establishing the last nursery in the industry in the long run is:

$$
W^{\prime}(n)-h_{n} \frac{W(n)+\delta G(\tau)}{\delta+h(n)}=0
$$

- Substituting for $W(n)$ and rearranging gives the socially optimal number of nursery firms in the long-run:

$$
n^{*}=\left(\frac{\Pi^{\prime}(n)+D}{D}\right) \frac{\delta+h(n)}{h_{n}}-\frac{\Pi(n)+\delta G}{D}
$$

- The introducer pays tax, $\chi$, internalizes the expected social cost of invasion and is a form of license fee


## Estimating the industry profit function

- For the US and Canada we used panel data to estimate:

$$
\pi(n)=b_{o}+b_{1}\left(\frac{L_{i t}}{n_{i t}}-F_{i t}\right)+\varepsilon_{i t}, b_{1}=(1-\gamma) / \gamma
$$

- The value of $\gamma$ was recovered as 0.7757 for the US and 0.1154 for Canada
- The results suggest that there is more differentiation in nursery products for the Canadian market compared to the US market


## Some parametric hazard functions



Time elapsed since introduction

## Variables for herbaceous species analysis $\left(a_{k}\right)$

| Name | Definition | Mean | Minimum | Maximum |
| :--- | :--- | :---: | :---: | :---: |
| Continent | Number of continents <br> covered by native range | 2 | 1 | 4 |
| Global | Number of global <br> bioregions already invaded | 5 | 0 | 24 |
| Annual | Plant form is annual <br> (vs. perennial, etc.) | 0.3 | 0 | 1 |
| Flower | Length of flowering period <br> in weeks | 14.4 | 8 | 45 |
| Polyploidy | (reproduce singly) <br> Has more than two sets of <br> chromosomes per nucleus | 0.6 | 0 | 1 |
| Abiotic | Fruit is dispersed <br> abiotically (vs. biotically) | 0.85 | 0 | 1 |
| Germno | Has no specific | 0.48 | 0 | 1 |

## Component matrix for PCA of herbaceous

 plant characteristic variables| Variable | Component |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
|  |  |  |  |  |
|  | FS1 |  | FS2 |  |
| Continents | .759 | -.113 | FS3 | FS4 |
| Global | .668 | -.043 | .547 | -.052 |
| Polyploidy | .597 | .240 | -.025 |  |
| Abiotic | .147 | .734 | -.108 | .212 |
| Annual | -.216 | .643 | .464 | .037 |
| Flower | -.088 | -.039 | .841 | .151 |
| Selfcompatible | .009 | .209 | -.035 | .035 |
| Germno | -.136 | .501 | -.231 | .869 |

Regression results for herbaceous species using PCA hazard model (Dependent var. is "duration")

| Variable | All Covariates |  |  |  | Only Significant Covariates (if any) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Weibull |  | Exponential |  | Weibull |  | Exponential |  |
|  | Coefficient | $\begin{gathered} p \\ \text { value } \end{gathered}$ | Coefficient | $\begin{gathered} p \\ \text { value } \end{gathered}$ | Coefficient | $p$ value | Coefficient | $\begin{gathered} p \\ \text { value } \end{gathered}$ |
| ONE | 5.300 | 0.000 | 5.315 | 0.000 | 5.299 | 0.000 | 5.313 | 0.000 |
| FS1 | -0.221 | 0.054 | -0.252 | 0.067 | -0.221 | 0.054 | -0.251 | 0.067 |
| FS2 | 0.256 | 0.014 | 0.279 | 0.023 | 0.256 | 0.014 | 0.278 | 0.023 |
| FS3 | -0.254 | 0.010 | -0.275 | 0.021 | -0.257 | 0.009 | -0.278 | 0.020 |
| FS4 | -0.014 | 0.896 | -0.023 | 0.861 |  |  |  |  |
| N | 106 |  | 106 |  | 106 |  | 106 |  |
| $\varphi$ parameter | 0.005 |  | 0.005 |  | 0.005 |  | 0.005 |  |
| $p$ parameter | 1.144 |  | 1.000 |  | 1.145 |  | 1.000 |  |
| LL | -140.298 |  | -141.199 |  | -140.307 |  | -141.217 |  |

Simulated optimal tax and number of nurseries selling a new exotic herbaceous species ( $\varphi=0.009$ )


## Summary of simulation results

- We developed a general MC framework to model the private and socially optimal number of firms in the horticulture industry when there is a risk of bioinvasion
- We then determined the optimal 'introducer pays' tax to internalize the externality
- The outcome is highly sensitive to the share of individual exotic plant sales in final profits
- Optimal US industry size is more sensitive to the tax because of greater substitutability $\left(\gamma_{\mathrm{US}}>\gamma_{\mathrm{C}}\right)$ \& lower CS
- An annual license fee would raise substantial revenues that could cover damage costs from a future invasion and fund screening programs for newly introduced species


